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Estimating the risk of re-emergence after stopping polio vaccination

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Abstract

Live vaccination against polio has effectively prevented outbreaks in most developed countries for more than 40 years, and there remain only a few countries where outbreaks of poliomyelitis by the wild strain still threaten the community. It is expected that worldwide eradication will be eventually achieved through careful surveillance and a well-managed immunization program. The present paper argues, however, that based on a simple stochastic model the risk of outbreak by a vaccine-derived strain after the cessation of vaccination is quite high, even if many years have passed since the last confirmed case. As vaccinated hosts are natural reservoirs for virulent poliovirus, the source of the risk is the vaccination itself, employed to prevent the outbreaks. The crisis after stopping vaccination will emerge when the following two conditions are met: the susceptible host density exceeds the threshold for epidemics and the vaccinated host density remains large enough to ensure the occurrence of virulent mutants in the population. Our estimates for transmission, recovery, and mutation rates, show that the probability of an outbreak of vaccine-derived virulent viruses easily exceeds 90%. Moreover, if a small fraction of hosts have a longer infectious period, as observed in individuals with innate immunodeficiency, the risk of an outbreak rises significantly. Under such conditions, successful global eradication of polio is restricted to a certain range of parameters even if inactive polio vaccine (IPV) is extensively used after the termination of live vaccination.

1. Introduction

The World Health Organization (WHO) has a target to interrupt wild poliovirus transmission throughout the world by 2013 (WHO, 2010). The number of patients with poliomyelitis by wild type poliovirus infection has decreased drastically due to a program using live oral polio vaccine (OPV). Immunity by OPV is defensible against excreted viruses because the major antigenic sites on the viral genome are relatively conserved between serotypes during replication (Minor, 1992). However, nucleotide substitutions responsible for increased neurovirulence frequently occur during replication in the human gut (Poyry *et al.*, 1988; Dunn *et al.*, 1990; Abraham *et al.*, 1993; Kew *et al.*, 1998; Matsuura *et al.*, 2000; Shulman *et al.*, 2000). It has been reported since the 1960's that the vaccine-derived strain excreted from humans can exhibit pathogenicity (Benyesh-Melnick *et al.*, 1967; Marker Test Subcommittee. The Japan Live Poliovaccine Research Commission, 1967). This suggests the possibility that vaccine-derived viruses could cause a poliomyelitis outbreak in a susceptible population after the cessation of an OPV program (Wood *et al.*, 2000). The objective of this study was to estimate the risk of outbreak of vaccine-derived strains after stopping OPV. While the number of attenuated virus carriers, the source of neurovirulent viruses, would decline after the discontinuation of OPV, the number of susceptible hosts would increase and may finally exceed the threshold for an outbreak. Therefore, successful eradication depends on which of these processes is faster. We

calculated the probability of successful global eradication, that is, the probability that the last carrier will be recovered before the population could experience an outbreak.

It will be shown below that the mean excretion period from an infected individual is one of the key factors that determine whether or not eradication fails. Except for immunodeficient individuals, virus is excreted from humans for approximately 1-3 months after OPV administration to a susceptible host (Alexander *et al.*, 1997). Excreted viruses are often virulent. For example, Yoshida *et al.* showed that type 3 vaccine-derived polioviruses isolated from an environment in Japan had high neurovirulence (Yoshida *et al.*, 2000). These strains were isolated from river or sewage waters approximately 3 months after routine OPV administration, showing that vaccine-derived strains could circulate in the human community. Other studies showed silent circulation of vaccine-derived strains occurred in the human community (Zdrazilek *et al.*, 1982; Miyamura *et al.*, 1992).

To avoid risks such as contact infection or vaccine-associated paralysis (VAP), inactivated polio vaccine (IPV) has been used in several countries (Murdin *et al.*, 1996). The USA switched its immunization strategy from OPV to IPV in 2000 (American Academy of Pediatrics Committee on Infectious Diseases, 1999). As IPV immunized hosts can be infected by polioviruses and excrete infectious virus, IPV is less effective than OPV in preventing infection, though numbers of excreted viruses are greatly reduced (Fine and Carneiro, 1999). Our study also investigated whether switching to IPV after the cessation of OPV effectively reduced outbreak risk.

The Pan American Health Organization (PAHO) reported a poliomyelitis outbreak by a type 1 vaccine-derived strain in Haiti and the Dominican Republic in July 2000 (Centers for Disease Control and Prevention, 2000). In the Latin American region, poliomyelitis caused by a wild strain was last reported in Peru in 1991, and eradication of poliomyelitis was declared in 1994. The recent outbreak in Haiti and the Dominican Republic could be ascribed to the decreased rate of OPV coverage and the spread of a neurovirulent vaccine-derived strain.

The polio eradication program plans to stop administering OPV after disappearance of the wild strain. If vaccine-derived strains remain when herd immunity falls below the epidemic threshold, outbreak by these strains could occur. In this paper, we study the probability of disease re-emergence caused by a vaccine-derived strain using a simple mathematical model. Epidemiological and genetic parameters, such as transmission rate, mean excretion period, mutation rate from attenuated to neurovirulent strains, are varied around estimated values (Gelfand *et al.*, 1959; Benyesh-Melnick *et al.*, 1967; Dunn *et al.*, 1990; Fine and Carneiro, 1999), and dependence on the probability of eradication detailed. In assessing the risk we assumed the following:

1. That the excretion period of vaccine-derived neurovirulent viruses can be longer than that of the attenuated viruses used in live immunization. Likewise, the

transmission rates of vaccine-derived strain can be greater than that of the attenuated strain. When hosts recover from infection by either viral strain, the degree of immunity is as effective as that raised by OPV immunization.

2. That infection by either the vaccine-derived or attenuated poliovirus can occur in IPV-immunized hosts. However, the number of secondary transmissions from a previously IPV-immunized host is smaller than that from a susceptible host, and the mean excretion period is shorter in an IPV-immunized host than in a susceptible host.
3. That when re-infection occurs in an individual immunized by OPV, excretion from the re-infection is ignored because the amount of virus excretion is negligibly small (Abraham *et al.*, 1993).
4. That antigenic drift does not occur. The focus of the study is on the risk of outbreak by a neurovirulent vaccine-derived strain with unchanged antigenic properties.
5. That a constant fraction (e.g. 70%) of hosts is efficiently immunized (seroconverted) before OPV is stopped, and that the population at that time is in endemic equilibrium under constant OPV coverage.

We first examine the risk of outbreak after OPV cessation (in the absence of an alternate program); second, we evaluate the effect of host heterogeneity on excretion duration; and third, we examine outbreak risk where extensive IPV-immunization follows OPV cessation.

Mathematical modeling is a powerful tool in the understanding of epidemiological dynamics (Anderson and May, 1991). Previous models of polio eradication have considered neither the re-infection by vaccine-derived strains of IPV-immunized hosts nor mutation giving rise to neurovirulent strains (Eichner and Hadelar, 1995; Eichner and Dietz, 1996). Our model allows for the mutation of attenuated strains to virulent strains while replicating in the human gut (Poyry *et al.*, 1988; Dunn *et al.*, 1990; Abraham *et al.*, 1993; Kew *et al.*, 1998; Matsuura *et al.*, 2000; Shulman *et al.*, 2000), and also allows both strains to infect IPV-immunized hosts. The probability for the success of global eradication is then calculated based on the stochastic model of epidemiological dynamics.

2. Material and Methods

We attempted to determine the risk of virulent poliovirus outbreaks after stopping live vaccination. Time $t=0$ represents the point at which immunization by live-poliovirus vaccine (OPV) is stopped. With a sufficiently high rate of immunization, the great majority of the population at time $t=0$ would be OPV-immunized hosts, which neither the attenuated (Sabin) nor virulent strain could infect. We first examined the risk where no alternative program followed OPV cessation. The effect

of extensive administration of inactive vaccine (IPV) following OPV discontinuation will be discussed later.

2.1. Deterministic epidemiological dynamics

The number of carriers of attenuated virus would decline after the end of a live vaccination program. Poliovirus is considered to have been eradicated when the last carrier had recovered. However, while the number of carriers declines, the number of hosts immunized by the live vaccine declines also. When the number of susceptible hosts exceeds a certain threshold, the way is opened for the spread of a virulent poliovirus. Thus, the risk of outbreak critically depends on the speed at which carrier numbers, as the source of virulent mutant virus, decrease and the speed at which susceptible hosts increase. Therefore, we need to keep track of the changes over time of the following demographic variables: the fraction of susceptible hosts (x), hosts infected with or carrying attenuated virus (y), virulent-virus infected hosts (v), and OPV-immunized hosts not carrying virus (z), with $x + y + v + z = 1$. The population size K is kept constant over time. A virulent virus strain can emerge through mutation in attenuated virus carriers. The probability of successful eradication, or conversely, the probability of an outbreak by a virulent virus, can be evaluated by constructing a stochastic process for the change in the number of infected hosts. To construct the stochastic process, we first derive the corresponding deterministic dynamics.

2.1.1. Deterministic dynamics before the cessation of OPV

Under the immunization of oral polio vaccine to newborns the dynamics for x , y and v are

$$dx / dt = -(\beta_a y + \beta_v v)x - ux + u(1 - p), \quad (1a)$$

$$dy / dt = \beta_a xy - (u + \gamma_a)y - \mu y + up, \quad (1b)$$

$$dv / dt = \beta_v xv - (u + \gamma_v)v + \mu y, \quad (1c)$$

$$dz / dt = \gamma_a y + \gamma_v v - uz, \quad (1d)$$

where t denotes the time variable in units of weeks, p is the immunization fraction to newborns (the fraction to be immunized times the seroconversion rate), u is the natural mortality of the host, β_a and β_v are the transmission rates of attenuated and virulent virus, respectively, $1/\gamma_a$ and $1/\gamma_v$ are the mean durations of attenuated and virulent virus infection, respectively, and μ is the mutation rate from attenuated to virulent virus (Fig 1). The number of births and deaths are balanced so that the total population is kept constant (K), and we focus on the changes in the fraction of each class, by which we can omit Eq. (1d) from the analysis. If $\mu = 0$, the condition for virulent or wild polio virus being wiped out from the population is that

$$p > p_c = \left(1 - \frac{1}{R_v}\right) \left(1 - \frac{R_a}{R_v}\right), \quad (2)$$

where $R_v = \beta_v / (u + \gamma_v)$ and $R_a = \beta_a / (u + \gamma_a)$ are the basic reproductive ratios of virulent and attenuated viruses (see, for example, Nowak and May, 2000). The threshold immunization fraction necessary for the eradication of virulent viruses is lower than that without circulation of attenuated viruses ($\tilde{p}_c = 1 - 1/R_v$). Thus silent circulation of attenuated virus can significantly increase the efficiency of vaccination. With nonzero mutation rate $\mu > 0$, both the attenuated and the virulent virus are maintained in the population:

$$\hat{y} = \frac{u}{(u + \gamma_a)} \frac{p}{\{(1 - R_a \hat{x}) + \tilde{\mu}\}}, \quad (3a)$$

$$\hat{v} = \frac{u}{(u + \gamma_v)} \frac{p}{\{(1 - R_a \hat{x}) + \tilde{\mu}\}} \frac{\tilde{\mu}}{(1 - R_v \hat{x})}, \quad (3b)$$

where $\tilde{\mu} = \mu / (u + \gamma_a)$ and \hat{x} is a positive root of

$$\begin{aligned} & R_a R_v \hat{x}^3 - (R_a + R_v + R_a R_v + \tilde{\mu} R_v) \hat{x}^2 \\ & + [(1 + \tilde{\mu}) + R_a + (1 - p + \tilde{\mu}) R_v] \hat{x} - (1 - p)(1 + \tilde{\mu}) = 0. \end{aligned} \quad (3c)$$

Figure 2 shows how the equilibrium numbers defined above depend on the immunization fraction p and the mutation rate μ , together with the mean number of virulent virus infections per week, $\beta_v \hat{x} \hat{v}$, under immunization.

As we will see later, the success or failure of global eradication after the cessation of OPV critically depends on the equilibrium densities of susceptible, attenuated virus infected, and virulent virus infected hosts at the time of stopping OPV illustrated above. Their parameter dependences are best described if there was no significant difference in transmission rates and recovery rates between attenuated and virulent polio strains, such that we can assume $\beta = \beta_a = \beta_v$, and $\gamma = \gamma_a = \gamma_v$. This is an important special case that is also partly supported from the data (see later). If this is the case, the dynamics (1) could be described by only two variables: x (the fraction of susceptible hosts) and $w = y + v$ (the fraction of hosts infected by either attenuated or virulent virus). The epidemiological dynamics (1) under OPV immunization are then

$$\begin{aligned} dx / dt &= -\beta x w - u x + u(1 - p), \\ dw / dt &= \beta x w - (u + \gamma) w + u p. \end{aligned} \quad (4)$$

from which the equilibrium fractions \hat{x} and \hat{w} are obtained:

$$\hat{x} = \left[R_0 + 1 - \sqrt{(R_0 - 1)^2 + 4pR_0} \right] / 2R_0,$$

$$\hat{w} = \left[u / (u + \gamma) \right] (1 - \hat{x}), \quad (5)$$

where $R_0 = \beta / (u + \gamma)$ is the basic reproductive ratio of both strains. If R_0 is sufficiently large ($R_0 \gg 1$),

$$\begin{aligned} \hat{x} &\approx \frac{1-p}{R_0}, \\ \hat{y} &\approx \frac{u}{u+\gamma} \frac{p}{p+\tilde{\mu}}, \\ \hat{v} &\approx \frac{u}{u+\gamma} \frac{\tilde{\mu}}{p+\tilde{\mu}}, \end{aligned} \quad (6)$$

which describe well how the equilibrium densities change with the immunization fraction p and mutation rate $\mu = (u + \gamma)\tilde{\mu}$ in the right panels of Fig. 2 (for $\beta_a = \beta_v$).

2.1.2. Deterministic dynamics after the cessation of OPV

The epidemiological dynamics for x , y and v after stopping OPV are

$$\begin{aligned} dx/dt &= -(\beta_a y + \beta_v v)x - ux + u, \\ dy/dt &= \beta_a xy - (u + \gamma_a)y - \mu y, \\ dv/dt &= \beta_v xv - (u + \gamma_v)v + \mu y, \end{aligned} \quad (7)$$

where t is now the number of weeks after OPV is stopped (Fig. 3). We assume that the population was in endemic equilibrium at time $t = 0$ under a constant fraction p of newborns immunized by OPV. As before, if we can assume that the transmission rates and recovery rates of attenuated and virulent polio strains are the same: $\beta = \beta_a = \beta_v$ and $\gamma = \gamma_a = \gamma_v$, the dynamics can be described by only two variables: x and $w = y + v$,

$$dx/dt = -\beta xw - ux + u, \quad (8a)$$

$$dw/dt = \beta xw - (u + \gamma)w. \quad (8b)$$

The susceptible density increases with time, while the densities of attenuated or virulent virus infected hosts decrease with time as long as $t > t_c$, where t_c is the time at which the susceptible density hits the epidemiological threshold: $x(t_c) = (u + \gamma) / \beta$ (see Fig. 3). The poliovirus infected density then starts increasing again. The question we ask in the following is whether the poliovirus goes to extinction around the time $t = t_c$ where its density approaches the minimum. In the following we derive the global eradication probability of poliovirus by analyzing the stochastic analog of dynamics (7) for $\beta_a < \beta_v$ or $\gamma_a > \gamma_v$, and that of the dynamics (8) for the special case of $\beta_a = \beta_v$ and $\gamma_a = \gamma_v$.

2.2. Probability of successful eradication

We then examine the probability of poliovirus eventually being lost from a population without causing an outbreak. To calculate extinction probabilities, we consider discrete time dynamics corresponding to (8) with weeks as time units. We assume that the number of secondary infections from a virulent-virus-infected host per week follows the Poisson distribution with mean $\beta Kx(t)$, where K is the total population size. The probability that the progeny of a virulent virus strain found in an infected host at time t eventually goes to extinction by chance before causing an outbreak is defined as $q(t)$. We also define $1-q(t)$ as the marginal risk of outbreak at time t , which is the probability that an infected host present at time t harbors the viruses whose progeny will cause outbreaks in the future. If $\beta_a = \beta_v = \beta$ and $\gamma_a = \gamma_v = \gamma$, the extinction probability $q(t)$ then satisfies the recursive equation

$$q(t) = \left[(1-\delta)q(t+1) + \delta \right] \exp \left[-\beta Kx(t)(1-q(t+1)) \right], \quad (9)$$

where $\delta = u + \gamma$ (see Appendix 1 for the derivation). The extinction probability $q(t)$ for arbitrary time t can be determined by solving (9), with $x(t)$ obtained from (5) and (8). The boundary condition for the recursion (9) is chosen at the time at which the fraction x of susceptibles first approaches a local maximum x_e at $t = t_e$ (x_e and t_e always exist because the deterministic trajectory of (8) approaches an endemic equilibrium with damped oscillations - see Fig. 3):

$$q_e = \left[(1-\delta)q_e + \delta \right] \exp \left[-\beta Kx_e(1-q_e) \right], \quad (10)$$

where $q_e = q(t_e)$ is the extinction probability at $t = t_e$.

The probability of eventual eradication can then be calculated as follows. We choose a reference time point $t = t_s$ before the deterministic trajectory for w reaches its minimum (see Fig. 3), at which the number of infected hosts $Kw_s = Kw(t_s)$ was large enough so that eradication before that time point could be ignored, but small enough so that competition between different viral lines could be ignored. According to extensive Monte Carlo simulations we found that the stochastic loss of the infecteds may occur only after their expected number falls below 100 or less. Noting this and the fact that the competition between viral strains can be ignored when $Kw_s / K \ll 1$, we chose $Kw_s = 100$. The probability of eventual extinction is then

$$P_{ext} = q(t_s)^{Kw_s}, \quad (11)$$

i.e. poliovirus eventually goes to extinction without causing outbreaks if and only if all progenies of the viruses present at $t = t_s$ go to extinction. Note that if the total population is subdivided into mutually isolated communities (e.g., 100 cities each with one million population), then the probability that none of the cities experiences the outbreak is given by (11) with $K = 100 \times \text{one million}$.

We conducted extensive Monte Carlo simulations of the fully stochastic process to check the accuracy of formula (11). For the Monte Carlo simulations, week by week changes in numbers of susceptibles, attenuated virus infecteds, and virulent virus infecteds in population of size K were followed. The changes between weeks caused by infection, recovery, mutation, and host mortality were generated by binomial pseudo-random numbers with the rates given by the dynamics (7). As shown below, the formula (11) for the probability of eventual eradication agreed quite well with that observed in the Monte Carlo simulations for 1000 independent runs.

2.3. Epidemiological parameters

The probability of global eradication depends on epidemiological, host demographic, and genetic parameters. Thus, estimates of the recovery rate γ , the transmission rate β , and the mutation rate μ are critical. All parameters used in the model were scaled in units of weeks.

2.3.1. Recovery rate γ , or the reciprocal of the mean excretion period.

The mean excretion duration after challenge with 6 logs of Sabin type 1 virus has been estimated to be 20.4 days for hosts not previously immunized, 12.3 days for previously IPV-immunized hosts, and 4.6 days for previously OPV-immunized hosts (Fine and Carneiro, 1999). Thus, the mean infectious period of a type 1 primary infection is about 3 weeks. While type 2 poliovirus showed a similar excretion period to type 1, type 3 has a significantly longer excretion period (Vaccine Administration Subcommittee. The Japan Live Poliovaccine Research Commission, 1966). Mean excretion periods are estimated as 20.5, 20.6, and 38.6 days for types 1, 2 and 3, respectively, for TOPV (trivalent oral polio vaccination) (Gelfand *et al.*, 1959). Regarding the risk of reemergence, type 3 poliovirus would be the most likely agent to persist and circulate longest after stopping OPV, and hence cause outbreaks. Therefore we adopted the excretion period for type 3 in assessing outbreak risk. Thus, we varied the recovery rate around $\gamma_a = 0.18$ per week, corresponding to 5.5 weeks as the mean excretion period. Because of the similarity between the recovery rates for attenuated (γ_a) and virulent (γ_v) polio infections, we also assumed $\gamma_v = 0.18$. A constant recovery rate assumed here implies that the infectious period has the long tail in an exponential distribution. The effect of tail in the infectious period will be examined later.

2.3.2. Transmission rate β , or the mean number of secondary infections.

While the probability of within-family infection was estimated to be 0.5 per case (Benyesh- Melnick *et al.*, 1967), we also needed to evaluate the mean transmission rate to other members of the community. The mean transmission rate was estimated from the basic reproductive rate: $R_0 = \beta / (u + \gamma) \approx \beta / \gamma$. The basic reproductive ratio of wild polioviruses in England and Wales during the pre-vaccination period has been

estimated to be $R_0 = 10-12$ (Anderson and May, 1991). More recent estimates have been $R_0 = 10-15$ in countries with poor sanitation and hygiene, and R_0 less than 10 in countries with good sanitation and hygiene (Fine and Carneiro, 1999). If we assume $\gamma = 0.18$, this gives estimates of $\beta = 1.8-2.7$ per week in developing countries. Much higher R_0 's of more than 20 have been reported by studies of poliomyelitis outbreaks over the past 20 years (Patriarca *et al.*, 1997). Because of this large variance in the estimated β , we varied the value rather widely, from 2 to 6, to evaluate eradication probability.

2.3.3. Mutation rate μ from the attenuated to the virulent virus

It is known that virulent mutants appear after replication in the human gut. Such virulent strains have caused outbreaks in populations with low OPV coverage in Haiti, the Dominican Republic and Egypt (Centers for Disease Control and Prevention, 2000, 2001). Dunn *et al.* reported that at least one viral serotype excreted from a susceptible individual immunized by OPV had mutated completely within 28 days (Dunn *et al.*, 1990). Thus, the mutation rate from attenuated to virulent viruses appeared to be high, in the order of $\mu = 0.1$ per week.

3. Results

Before proceeding to specific parameter dependences, it should be noted that the time at which the fraction of susceptible hosts exceeds the threshold for epidemics is crucial in understanding the problem. The number of virulent-virus-infected hosts increases if the fraction of susceptible hosts is larger than the threshold $x_c = (u + \gamma) / \beta$, which is the reciprocal of the basic reproductive rate $R_0 = \beta / (u + \gamma)$, and decreases when x is smaller than x_c . During the initial period, when the fraction of OPV-vaccinated individuals is large, the fraction of susceptibles is less than the threshold x_c , so that the risk of an outbreak is negligible, even though considerable numbers of virulent mutants are being generated at each time step. The number of virus carriers decreases during the period from the cessation of OPV to time t_c at which the susceptible density exceeds the threshold x_c . If the number of carriers becomes zero around t_c , polio will be globally eradicated. However, if virus survives this 'endangered' period around t_c , the infected density increases again and a future outbreak becomes certain. The following formula (derived in Appendix 2) provides an approximate time t_c and minimum infected fraction w_c as a function of epidemiological parameters:

$$t_c \approx Lp / R_0, \quad (R_0 \gg 1), \quad (12a)$$

$$Kw_c \approx K \frac{D}{L} \exp \left[-\frac{p^2}{2R_0} \frac{L}{D} \right], \quad (R_0 \gg 1, L \gg D), \quad (12b)$$

where $D = 1/\gamma$ is the mean duration of infection, $L = 1/u$ the life expectancy of the host, and $R_0 = \beta / (u + \gamma)$ the basic reproductive ratio. There is a high probability of

global eradication if Kw_c is sufficiently smaller than 1; whereas, there is a high risk of re-emergence if Kw_c is greater than 10. Although assessment of outbreak risk should be based on the probability of global viral extinction as discussed below, the above approximate formula gives insights into the likelihood of reemergence and parameter dependence on eradication probability. It also gives an accurate estimate of the critical time t_c at which either global eradication occurs or an outbreak starts.

3.1. Paths to extinction and paths to outbreak

Figure 3 shows deterministic changes in fraction x of susceptibles and fraction $w = y + v$ of poliovirus carrying hosts after cessation of live vaccination. The fraction of susceptibles exceeded the epidemiological threshold x_c around time $t = t_c (= 150)$ weeks after live-vaccination discontinuation. When the fraction of susceptibles exceeds the epidemiological threshold, the fraction of infecteds is at its minimum. The public health objective is to make the number of infecteds zero around time $t = t_c$. Figure 4 illustrates sample paths for the stochastic process corresponding to the deterministic trajectory in Fig. 3. In this example, 61 out of 100 independent runs led to the global eradication of poliovirus (i.e. the number of infected hosts hit the absorbing boundary at zero). However, in the remaining runs, poliovirus escaped extinction around $t = t_c$, increased again, leading to an outbreak by a virulent strain. The probability of successful eradication is thus 61% by the parameter set used in Fig. 4.

3.2. Parameter dependence

Figure 5 illustrates how the probability of the failure of global eradication $P_{fail} = 1 - P_{ext}$ depends on each parameter, which we discuss in turn below. We set the following values as ‘standards’, and varied each of the parameters to see its effect. The fraction of immunized newborns before $t = 0$: $p = 0.7$; transmission rate of virulent virus: $\beta_v = 3.7$, that of attenuated virus: either $\beta_a = \beta_v$ or $\beta_a = \beta_v / 2$; recovery rate: $\gamma = 0.18$ (in both viruses); mutation rate from attenuated to virulent viruses: $\mu = 0.1$; natural host mortality: $u = 0.00025$ (all measured in units of weeks), and total population: $K = 100$ million. With the chosen values of β , u , and γ , the basic reproductive rate of polioviruses was $R_0 = 20$. In Fig. 5, lines indicate the eradication probability calculated from Eqs. (8)-(11) for $\beta_a = \beta_v$, the dots indicate the observed eradication probability for 1000 independent runs of the stochastic process corresponding to the deterministic model (7) for $\beta_a = \beta_v$, and the crosses indicate that for $\beta_a = \beta_v / 2$. We first discuss the results for $\beta_a = \beta_v$ in 3.2.1-3.2.5 below, and discuss the effect of a lower transmission rate of attenuated virus in 3.2.6.

3.2.1. The immunization fraction p before stopping OPV

The effect of fraction p of OPV-immunized newborns before stopping the live-vaccination is illustrated in Fig. 5(A). While the probability of failing eradication is

low when p is sufficiently high, it rises drastically around $p=0.7$ when p is decreased. For example, if the immunization fraction is 60% or less before OPV is stopped, future outbreak by virulent poliovirus is almost certain. There are two reasons why a lower p before stopping OPV enhances the risk of future outbreaks: First, it shortens the time for the susceptible host density to reach the epidemiological threshold, and second, it increases the initial infected density w_0 , thereby keeping the minimum density from extinction.

3.2.2. The recovery rate γ

The success of global eradication greatly depends on the recovery rate, or its reciprocal, the mean infectious period (Fig. 5(B)). The higher the recovery rate, the more rapidly the number of poliovirus carriers decreases after supply by OPV is stopped. It is then possible to make the expected number of infecteds negligibly small when the susceptible fraction exceeds the epidemiological threshold. Conversely, by having a longer infectious period (a lower recovery rate), viruses safely persist over the endangered period around $t=t_c$. In examples shown in Fig. 5(B), infectious periods of 7 weeks or longer are disastrous for eradication. In reality, the infectious period varies between hosts, such that in hosts with innate immunodeficiency the infectious period can be typically longer than 1 year (Hara *et al.*, 1981; Kew *et al.*, 1998). Even a tiny fraction of such hosts significantly increases the risk of virulent virus outbreaks, as we show later.

3.2.3. The transmission rate β

The effect of increasing the transmission rate (Fig. 5(C)) is parallel to decreasing the recovery rate described above, and both can be regarded as having the effect of increasing R_0 . However, decreasing the recovery rate affects eradication probability more sensitively than increasing the transmission rate, as the former contributes to slowing the decay rate for the number of virus carriers as well as increasing R_0 (see also Eq. 12).

3.2.4. The mutation rate μ from the attenuated to virulent viruses

The eradication probability is insensitive to the mutation rate from attenuated to virulent viruses (Fig. 5(D)). If viruses persist during the period around $t=t_c$, it does not matter which type survived as eventually the virulent virus increases its relative frequency in the viral population (if $\beta_v = \beta_a$). Quite different results follow when the attenuated virus has a lower transmission rate than the virulent virus (the crosses), where the probability of failing eradication is maximized for an intermediate mutation rate.

3.2.5. The total population size K

This has an obvious dependence on the risk of outbreaks. The larger the population size, the larger the probability that viruses are not lost during the endangered period, and hence, the larger the risk of outbreaks. In the example shown in Fig. 5(E), a population of 10 million individuals has a more than 90% of chance for successful eradication, but communities of 100 and 1000 million have only 50% and less than 5% chances, respectively, using the same epidemiological parameters.

3.2.6. The transmission rate β_a of attenuated virus smaller than that β_v of virulent virus

In each panel of Fig. 5, the probability of failing global eradication when the transmission rate β_a of attenuated virus is half of that of virulent virus β_v is plotted as the cross-hatches. In all cases except for the dependence of mutation rate, a lower transmission rate of attenuated viruses *increases* the risk of virulent virus outbreak after the cessation of OPV. This rather counter-intuitive results follow from the fact that silent circulation of attenuated viruses under live vaccination helps increasing the efficiency of immunization, as we have seen in the comparison between the threshold immunization fractions with and without silent circulation (see (2)), and the equilibrium densities for $\beta_a < \beta_v$ (left panels of Fig. 2) and for $\beta_a = \beta_v$ (right panels). Decreasing the transmission rate of attenuated virus increases the density of susceptibles in the equilibrium population under vaccination, thus shortening the time until the susceptible density hits the epidemiological threshold after the cessation of OPV (compare Fig. 2(C) with 2(D)).

3.3. Tail of infectious period

A constant recovery rate assumed in the previous sections implies that the infectious period is exponentially distributed. One may suspect that an outbreak of vaccine-derived viruses a few years after the cessation of OPV might be the artefact caused by this long tail in the infectious period. We found, however, that the long tail in the infectious period is not necessary for this to happen --- it is the silent circulation of avirulent polio viruses in the population, commonly observed in nature and occurring in our model as well, that is responsible for the outbreak that occurs long after the cessation of OPV. To show this, we conducted numerical simulations in which we assume that the host recovers exactly 4 weeks after the infection, i.e. the distribution of infectious period has no tail at all. The infected hosts nevertheless persist in the population far longer than 4 weeks (the infectious period of an individual) after stopping OPV, which allows the outbreak of vaccine derived strain to occur a few years after the cessation (Fig. 6).

3.4. Marginal risk of outbreak

Figure 7 illustrates change over time in the marginal risk of viruses found at time t . Marginal risk is defined as $1 - q(t)$ -- the probability that an infected host present at time t harbors viruses whose progeny will cause a future outbreak. Marginal risk is negligibly small just after $t = 0$, and rapidly increases with t near $t = t_c$. In the parameters used in Fig. 7, the rate of increase in probability is the highest around $t = 150$ when the susceptible host density exceeds the threshold (see Fig. 3). However, the marginal risk of viruses before this point is by no means negligible as there is notable probability that progenies of viruses found during $t = 100$ to 150 would later cause an outbreak.

3.5. Effect of a high risk group

We here examine the case where a small fraction r of hosts has a recovery rate, γ' , much lower than γ for other hosts. In the simulation shown in Fig. 8, the recovery rate of most individuals was $\gamma = 0.2$. Using this value, successful eradication is certain (other parameters: transmission rate, $\beta = 2.5$; natural mortality, $u = 0.00025$; immunization fraction before stopping OPV, $p = 0.7$; total population, $K = 100$ million). When we assume only 0.01% of newborns have a 10-times longer infectious period than other members, i.e., $\gamma' = 0.1\gamma$, due to innate (World Health Organization, 1989; Fine and Carneiro, 1999), or acquired immunodeficiency, the probability of failure in global eradication rises to 79% (Fig. 8). Thus even a tiny fraction of high risk group drastically makes the global eradication difficult.

3.6. Effectiveness of IPV

What if extensive IPV-immunization follows the cessation of OPV? We assume in this case that all newborns are immunized by inactive vaccine before eventual eradication. The probability of global eradication is then evaluated in the light of the results obtained so far by replacing the transmission rates and recovery rates with values for previously IPV-immunized hosts instead of the values for susceptible hosts. IPV cannot prevent infection by either attenuated or virulent viruses, although it can reduce disease severity, and fewer viruses are excreted from IPV immunized hosts than from unvaccinated hosts (Henry *et al.*, 1966). IPV vaccination would therefore reduce the transmission rate and increase the global eradication probability (see Fig. 5(C)). Also, IPV immunization reduces the infectious period, again increasing the probability of successful eradication (Fig. 5(B)). However, these considerations assume that *all* hosts are IPV-immunized after the cessation of OPV. The actual amount of risk reduction by IPV depends on coverage, vaccine efficiency, and host heterogeneity in the excretion period.

4. Discussion

The PAHO and WPRO (Regional Office for the Western Pacific) declared the eradication of poliomyelitis in 1994 and 2000, respectively. Nevertheless, an outbreak of poliomyelitis caused by a type 1 vaccine-derived strain was reported in Haiti and the Dominican Republic in 2000 (Centers for Disease Control and Prevention, 2000), and an outbreak by a type 2 vaccine-derived strain has been reported in Egypt (Centers for Disease Control and Prevention, 2001), in Nigeria (Wassilak S *et al.*, 2011). It is assumed that both cases were due to the low rate of vaccine coverage. Although OPV or IPV immunization have been effective in controlling the transmission of wild-type strains, cases of re-emergence by wild-type strains have been reported in several countries (Patriarca *et al.*, 1997) in which inadequate vaccine potency or a high rate of unimmunized individuals led to low herd immunity in the population.

According to a review by Patriarca *et al.*, rates of seroconversion by OPV approached 100% for each serotype in industrialized countries, but were approximately 70% for types 1 and 3 in developing countries (Patriarca *et al.*, 1991). Many studies have demonstrated that interference by enteroviruses in human gut and other factors in OPV administration affect the seroconversion rate (Triki *et al.*, 1997). Thus, even if OPV coverage is as high as 90%, the immunized fraction p in our model becomes 62%, under the 70% seroconversion rate observed in developing countries. This should invoke serious concern if we recall that the reduction in immunization fraction p before cessation of OPV drastically increases the risk of outbreak, as shown in Fig. 5(A).

Our results have specifically shown that a herd immunity level of less than 60% before the cessation of OPV led to the failure of poliovirus eradication under typical epidemiological parameters adopted in this paper. This suggests that maintaining more than 90% OPV coverage is not enough to ensure successful eradication, and that every effort should be made to increase the seroconversion rate in developing countries. Another important parameter affecting the probability of eradication is the recovery rate γ estimated from the mean infectious period. Most data concerning virus excretion rates available from field studies were for the type 1 vaccine strain (Alexander *et al.*, 1997), while much less information is available for types 2 and 3. As type 2 and particularly type 3 have longer excretion periods than type 1, these strains are more likely to persist after cessation of OPV and be the causative agents of outbreaks. In assessing risk, we varied the recovery rate in the range $\gamma = 0.1 - 0.25$, based on estimates for the excretion period of type 3 poliovirus, which appears to have the longest excretion period. Whether this overestimates the risk will eventually be settled by more accurate estimations of excretion periods. However, there may not be enough time to allow the necessary studies, and action may need to be taken now assuming the worst possible scenario.

We have shown that even when the mean infectious period is far below the fatal level for eradication failure (e.g. less than 7 weeks in the example shown in Fig. 5(B)), the presence of a tiny fraction of immunodeficient individuals greatly increases the risk of disease reemergence. This was because the primary immunodeficient group acts as a long-term viral reservoir, allowing the virus to persist through the endangered period around t_c (which comes typically 150-200 weeks after the cessation of OPV). At present, no evidence exists whether secondary immunodeficient groups, such as HIV infected patients, could act as a long-term reservoir of poliovirus, but it is possible. Monitoring virus excretion from such high-risk groups would become critically important.

Another factor that drastically increases the risk of polio outbreak after the cessation of OPV is lower transmission rate β_a of attenuated viruses than that β_v of vaccine-derived virulent viruses, as we have shown in Fig. 5 where the results for $\beta_a = \beta_v / 2$ is compared with the case $\beta_a = \beta_v$. If we further reduces the transmission rate of attenuated viruses to $\beta_a = \beta_v / 4$, the risk of outbreak rises up still more (not shown). This rather unexpected and hazardous dependency comes from the fact that silent circulation of attenuated viruses under vaccination is beneficial in increasing the efficiency of herd immunity. The more is the transmission rate of attenuated viruses, the less is the fraction of hosts that remain susceptible under a fixed vaccination rate. Reducing the transmission rate of attenuated viruses thus increases the susceptible density under vaccination, and hence shortens the time until the susceptible density hits the epidemiological threshold after the cessation of OPV.

Transmission rates (β) can be estimated from R_0 , which in turn have been estimated from the mean host age at infection (Anderson and May, 1982; Patriarca *et al.*, 1997; Fine and Carneiro, 1999). Such surveys indicate that R_0 of vaccine-derived poliovirus lies in the range 5-25, depending on the hygiene levels of the region. This is well above the threshold $R_0 = 1$ that allows circulation in susceptible hosts. Eradication probability can be increased by reducing the transmission rate, i.e., by preventing vaccine-derived viruses from circulating in the population as much as possible. Public health attempts to reduce contact with infectious individuals becomes important in reducing the transmission rate β . At the same time, monitoring the circulation of shed virus in the healthy human population and environment becomes even more important after the last round of OPV.

Many studies have shown that immunity by IPV cannot prevent re-infection by poliovirus (Murdin *et al.*, 1996). However, IPV immunization reduces mean excretion duration by 40% compared to unimmunized cases, thus increasing the recovery rate γ by 67% (Henry *et al.*, 1966). IPV also reduces the transmission rate because the number of excreted viruses per unit time also declines. As a result of the increased γ and decreased β , the probability of eradication is higher if IPV immunization follows the cessation of OPV than if no program follows it. Although eradication cannot be

achieved without OPV, IPV should be considered, together with its high seroconversion rate, as the primary follow-up strategy after OPV cessation to prevent the secondary transmission of vaccine-derived virus (Ghendon and Robertson, 1994; Sutter *et al.*, 2000).

Neither escape-mutation by antigenic drift (Nowak and May, 1991; Nowak *et al.*, 1991; Sasaki, 1994; Haraguchi and Sasaki, 1997; Sasaki and Haraguchi, 2000) nor the emergence of vaccine-resistant strains (Anderson and May, 1991; McLean, 1995) is considered in this paper, though, in our analysis of IPV-immunization, both attenuated and virulent viruses can be regarded as IPV-resistant strains. The presence of multiple serotypes in the viral population complicates the eradication strategy (Lipsitch, 1997). The reason we have ignored such factors in this model of polio eradication is the observation that nucleotide divergence within the VP1 region, which includes the antigenic site, is less than 1.4% in vaccine strains, enabling the protection by OPV or IPV immunization (Matsuura *et al.*, 2000). In a study using a monoclonal antibody towards a vaccine strain, substitutions in the VP1 region did affect neutralization (Wiegers *et al.*, 1989). However, these vaccine-derived strains could still be neutralized by polyclonal antiserum (Matsuura *et al.*, 2000), or be prevented under well-maintained herd immunity (Iwai *et al.*, 2008).

Our model suggests that susceptible host density exceeds the threshold around the time $t_c \approx Lp/R_0$ after the cessation of OPV (e.g., $t_c = 140$ weeks when life expectancy $L = 1/u = 4000$ weeks, immunization fraction $p = 0.7$ and basic reproductive ratio $R_0 = 20$). During the dangerous period around t_c , additional surveillance systems other than normal AFP (acute flaccid paralysis) surveillance should be organized to reduce the risk of reemergence:

1. Seroepidemiological surveillance of the seroconversion rate within a population. For communities with low seroconversion rates, additional immunization by IPV should be offered. Herd immunity should be maintained at a level over 80% seroconversion.
2. Surveillance of the environment and of shed virus from the source of infection. Upon poliovirus isolation, immunization by IPV is to be administrated to the risk area.
3. Public health administration. A hygiene control program (hand washing practice, use of disposal diapers, etc.) would contribute to the reduction in transmission rate β , preventing the virus from circulating.
4. Monitoring of high-risk groups such as immunodeficient individuals.

It is very difficult to use IPV globally due to economic reasons and other administrative difficulties. IPV immunization in restricted regions and in at-risk communities, together with good surveillance systems and hygiene control programs, would be more practical tactics to globally extinguish vaccine-derived viruses.

Appendix 1: Derivation of Eq. (9)

Here we derive Eq. (9) in the text. This is derived by noting that there may be i infected hosts in the next time step either if an infected host gives rise to $i-1$ secondary infections and itself remains infected, or if it gives rise to i secondary infections and itself dies or recovers. Thus

$$\begin{aligned} q(t) &= (1-\delta) \sum_{i=1}^{\infty} \frac{\lambda(t)^{i-1}}{(i-1)!} e^{-\lambda(t)} q(t+1)^i + \delta \sum_{i=0}^{\infty} \frac{\lambda(t)^i}{i!} e^{-\lambda(t)} q(t+1)^i \\ &= [(1-\delta)q(t+1) + \delta] e^{-\lambda(t)(1-q(t+1))} \sum_{j=0}^{\infty} \frac{\{\lambda(t)q(t+1)\}^j}{j!} e^{-\lambda(t)q(t+1)} \\ &= [(1-\delta)q(t+1) + \delta] e^{-\lambda(t)(1-q(t+1))} \end{aligned} \quad (\text{A1})$$

with $\lambda(t) = \beta K x(t)$, which then leads to (9) in the text.

Appendix 2: Approximate time and number of infecteds at the minimum point

It is useful to obtain an explicit formula for the minimum number of infecteds and the time at which this number reaches its minimum in the deterministic trajectory. This clarifies the parameter dependence on the risk of re-emergence. We found the following approximation useful. We ignore the first term in the right hand of (8a), because it remains very small during the time interval from $t = 0$ to $t = t_c$, to give

$$x(t) = 1 - (1 - x_0)e^{-ut}, \quad (\text{A2})$$

(see, for example, Anderson and May, 1991). Integrating (8b) we have

$$w(t) = w_0 \exp \left[\int_0^t [\beta x(s) - (u + \gamma)] ds \right]. \quad (\text{A3})$$

Clearly $w(t)$ attains the local minimum when $t = t_c$ where $\beta x(t) = u + \gamma$. Letting

$$a = \frac{\beta - (u + \gamma)}{u} = k(R_0 - 1), \quad b = \frac{\beta(1 - x_0)}{u} = kR_0(1 - x_0), \quad (\text{A4})$$

with $k = (u + \gamma)/u$ and $R_0 = \beta/(u + \gamma)$, we therefore have

$$t_c \approx \frac{1}{u} \log \left[\frac{b}{a} \right] = L \log \left[\frac{R_0(1 - x_0)}{R_0 - 1} \right], \quad (\text{A5a})$$

$$w_c \approx w_0 \left(\frac{b}{a} \right)^a e^{-b} = w_0 \left(\frac{R_0(1 - x_0)}{R_0 - 1} \right)^{k(R_0 - 1)} \exp[R_0 x_0 - 1], \quad (\text{A5b})$$

where $L = 1/u$ is the life expectancy, and $R_0 = \beta/(u + \gamma)$ the basic reproductive rate. We expect a high probability of eradication if Kw_c is sufficiently smaller than 1, and show significant risk of re-emergence if it is 10 or more. The deviation of w_c from the true minimum is small in logarithmic scale, though it is as large as 50% in normal scale. However, for the purpose of quickly checking the likelihood of successful

692 eradication, this formula is useful. If we assume that x_0 and w_0 take the values at the
 693 endemic equilibrium with the vaccination rate p (Eq. (5) in the text), we obtain the
 694 asymptotic formula for large R_0 :

$$695 \quad t_c \approx Lp / R_0, \quad (R_0 \gg 1), \quad (\text{A6a})$$

$$696 \quad Kw_c \approx K \frac{D}{L} \exp \left[-\frac{p^2}{2R_0} \frac{L}{D} \right], \quad (R_0 \gg 1, L \gg D), \quad (\text{A6b})$$

697 where $D = 1 / \gamma$ is the mean duration of infection.

698

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842

843

Figure Legend

Figure 1. The schematic diagram of the epidemiological dynamics. β_a and β_v : the transmission rate of attenuated and virulent virus, γ_a and γ_v : the recovery rate of attenuated and virulent virus, μ : the mutation rate from attenuated to virulent virus, u : the host birth rate (= death rate), p : the fraction of newborns immunized by OPV. The flows by natural host mortality are omitted.

Figure 2. The densities in endemic equilibrium under the immunization fraction p . The number, $K\beta_v\hat{x}\hat{v}$ of hosts newly infected by virulent virus in a week (top row), the equilibrium number $K\hat{x}$ of susceptible hosts (second row), that $K\hat{v}$ of attenuated virus infected hosts (third row), and that $K\hat{v}$ of virulent virus infected hosts (bottom row) are plotted as a function of immunization fraction p for varying mutation rates μ for the emergence of virulent virus from an attenuated virus (solid: $\mu = 0.1$, dashed: $\mu = 0.01$, dot dashed: $\mu = 0.001$). The population size K is 100 million, $\beta_v = 2.5$ is the transmission rate of virulent virus. Left panels (A, B, E, G): The transmission rate of attenuated virus is half of that of virulent virus: $\beta_a = 1.25$. Right panels (B, D, F, H) β_a is the same as β_v . Other parameters are $\gamma_a = \gamma_v = 0.25$, $u = 0.00025$.

Figure 3. Deterministic trajectory after stopping OPV. Deterministic trajectory of epidemiological dynamics (8) in the text. The fraction $x(t)$ of susceptibles (upper panel) and the fraction $w(t)$ of infecteds (lower panel) are plotted as functions of the time $t = 0$ since the cessation of OPV. The dotted line indicates the threshold host density for outbreak: $x_c = (u + \gamma) / \beta$. The initial fractions x_0 and w_0 at time $t = 0$ are assumed to be in endemic equilibrium under OPV immunization to a constant fraction, p , of newborns. The time $t = t_c$ at which the fraction of infecteds is minimized in deterministic trajectory is indicated, together with time $t = t_s$ and $t = t_e$ defined for the calculation of the global eradication probability (Eq. (11)). Parameters are: $p = 0.7$, $\beta = 3.7$, $\gamma = 0.18$, $u = 0.00025$.

Figure 4. Sample paths for the number of infecteds observed in Monte Carlo simulations. Sample paths for the number of infecteds observed in Monte Carlo simulations of the stochastic process corresponding to dynamics (7). One hundred independent runs are illustrated by thin lines. Thick broken lines indicate the deterministic trajectory. The histogram shows the distribution for the times at which viruses went to extinction. 38 out of 100 runs never go to extinction, and cause outbreaks. The parameters are the same as in Fig. 3, and $K = 10^8$.

Figure 5. The probability of the failure of global eradication as a function of epidemiological and genetic parameters. Each panel shows how the probability of failing the global eradication $P_{fail} = 1 - P_{ext}$ (where P_{ext} is defined in Eq. 11) depends on a chosen parameter. Except for the varying parameter in each panel, the parameters are fixed as $p = 0.7$, $\beta = 3.7$ ($\beta_v = \beta_a = \beta$ for dots and lines, and $\beta_v = \beta$, $\beta_a = \beta/2$

for cross-hatched), $\gamma = \gamma_v = \gamma_a = 0.18$, $m = 0.1$, $K = 10^8$, and $u = 0.00025$. Varying parameters are: A) fraction p of OPV-immunization before its cessation, B) recovery rate γ , C) transmission rate β , d) mutation rate μ , e) total population size K . Lines: the probability of failure obtained from formula (11) in the text (for $\beta_v = \beta_a = \beta$), dots: the proportion of failing eradications in 1000 independent runs of the Monte Carlo simulation for $\beta_v = \beta_a = \beta$, and cross-hatched: that for $\beta_v = \beta$, $\beta_a = \beta/2$.

Figure 6. The effect of tail in the infectious period. A) The probability that the host remains infectious after it is infected at time 0. Dotted curve: the exponential distribution assumed in the previous sections with a constant recovery rate $\gamma = 0.25$ per week. Solid curve: the truncated distribution in which all the hosts recovers exactly 4 weeks after the infection. B) The Monte Carlo simulation results assuming the truncated distribution of the infectious period. The time change in the number of virus-infected hosts since OPV is stopped. The emergence of virulent virus occurs after 50-60 weeks after the secession of OPV. The parameters are $\beta_a = 2.5$, $\beta_v = 5$, $u = 0.00025$, $p = 0.6$, $\mu = 0.1$, and $K = 10^8$. The 'mean' infectious period is 4 weeks.

Figure 7. Marginal risk $1 - q(t)$ of outbreaks as a function of time t since OPV cessation. The marginal risk $1 - q(t)$ is defined as the probability that an infected host present at time t harbors viruses whose progeny will cause outbreaks in the future. $p = 0.7$, $\beta = 3.7$, $\gamma = 0.18$, $u = 0.00025$, $K = 10^8$.

Figure 8. The effect of a high-risk group on global eradication. One in ten thousand (0.01%) of hosts are assumed to be born having a longer excretion period (lower recovery rate γ') when infected by virus. Remaining hosts have the recovery rate γ . $\gamma' = 0.1\gamma$ and $\gamma = 0.2$ is assumed and values $p = 0.7$, $\beta = 2.5$, $\mu = 0.1$, $u = 0.00025$, $K = 10^8$ are used for other parameters. Without the high-risk group, i.e. when all hosts have the recovery rate $\gamma = 0.2$, global eradication is certain. However, with the addition of a fraction 0.01% of high-risk group in the population, eradication fails in 79 out of 100 independent runs, allowing the outbreak of virulent virus. A) Sample paths for the number of infecteds for 100 independent runs. Thick broken lines show the deterministic trajectory. B) Deterministic trajectories for the fraction of infected $w(t)$ when all hosts have the recovery rate γ (broken line), and when 0.01% of hosts have lower recovery rate γ' (solid line).

Figure 1

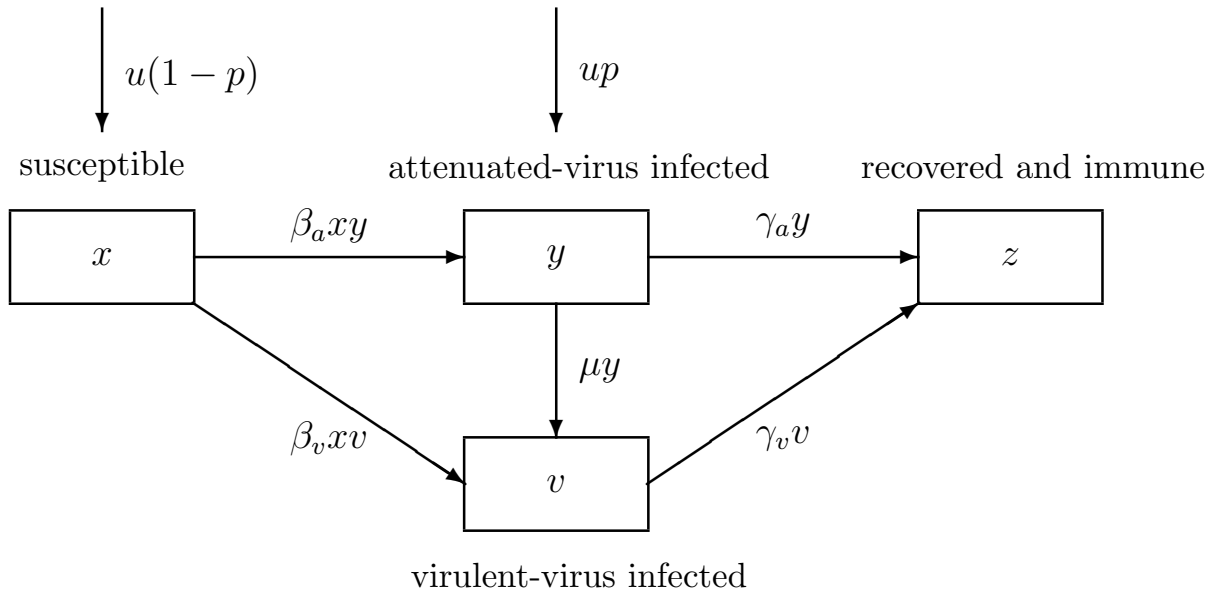


Figure 2

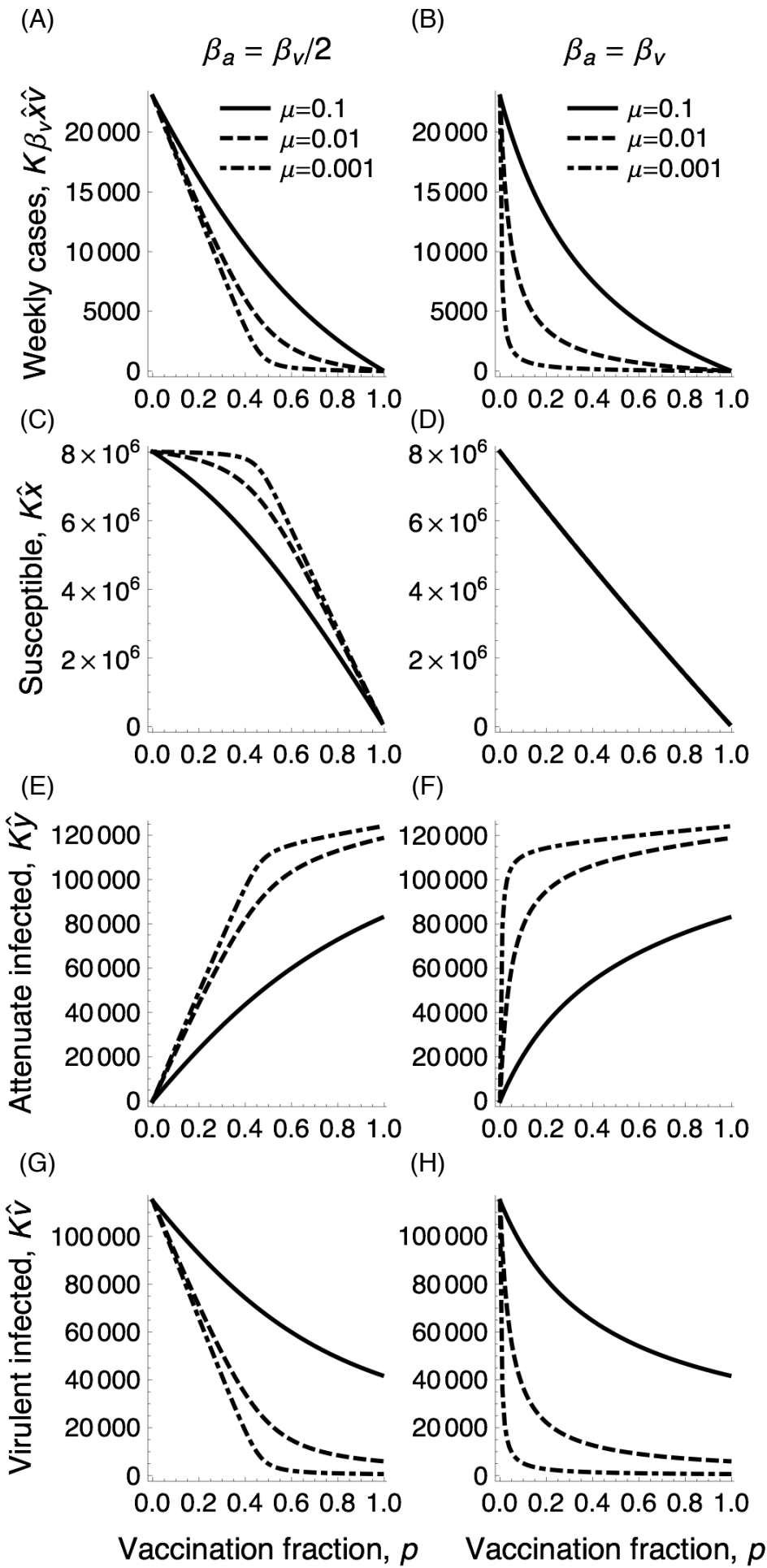
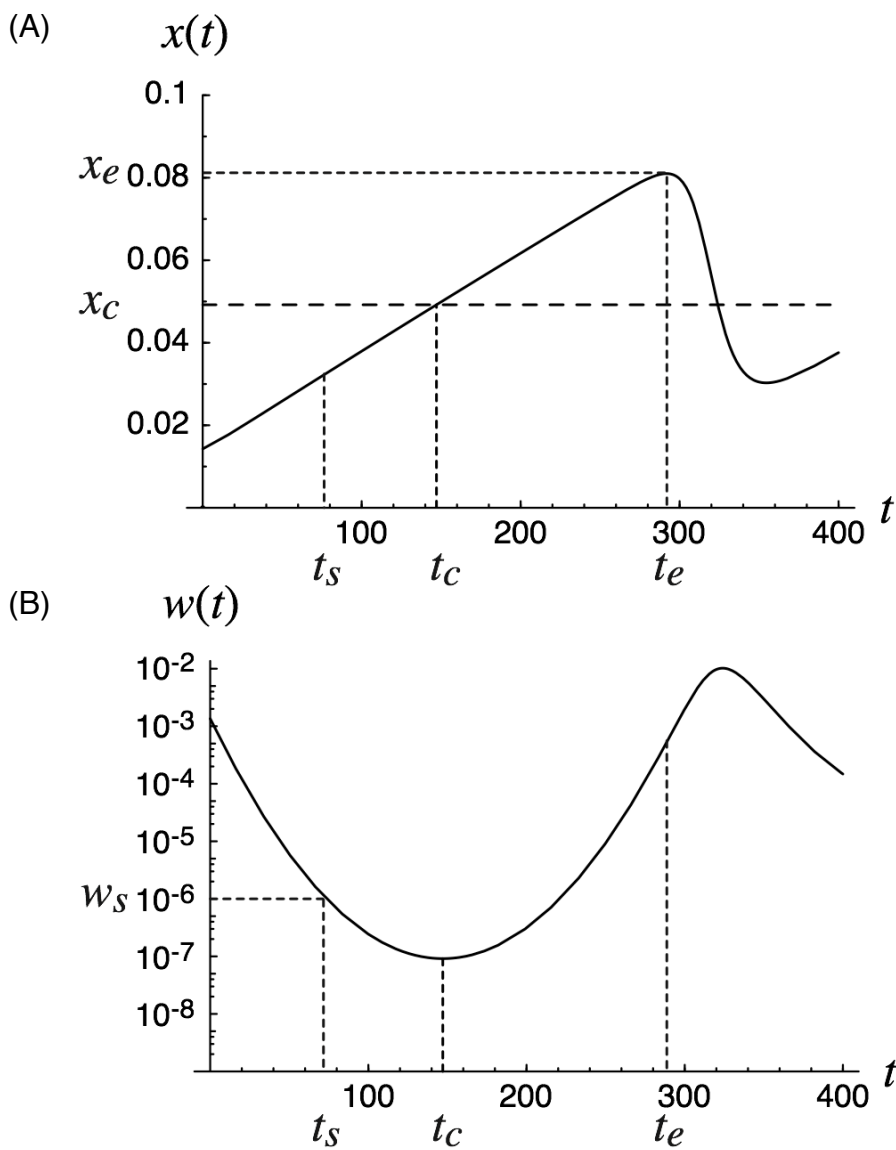
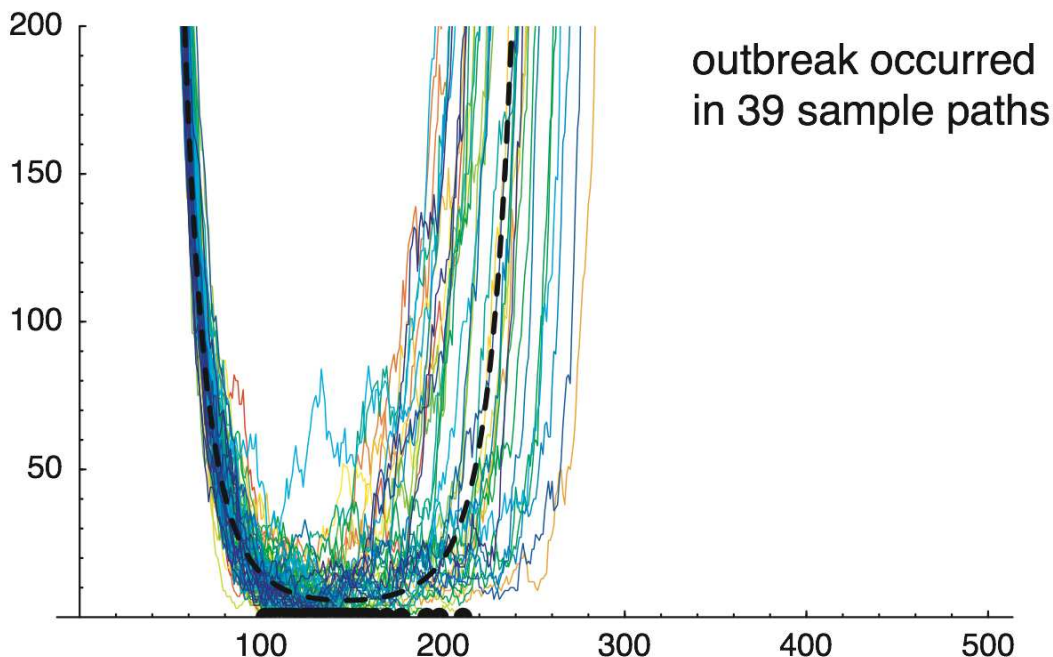


Figure 3



(A)

number of infected hosts

 $K_w(t)$ 

(B)

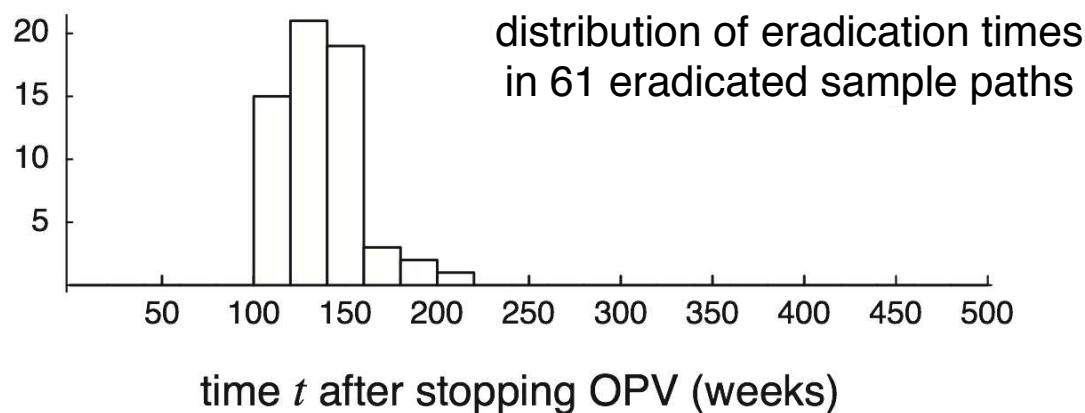


Figure 5

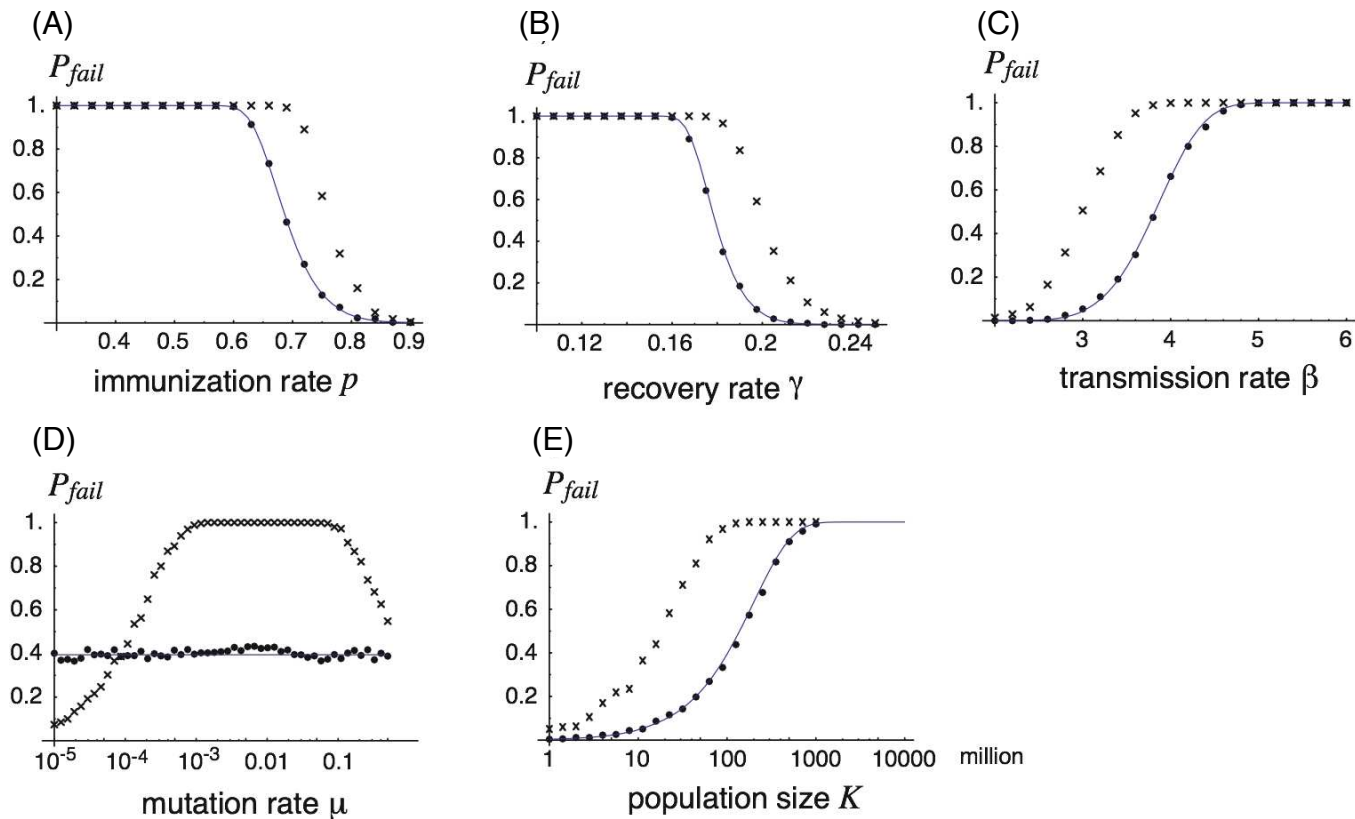


Figure 6

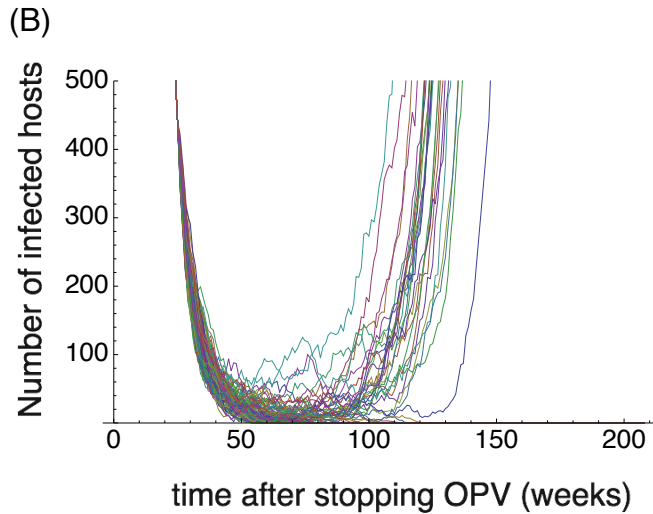
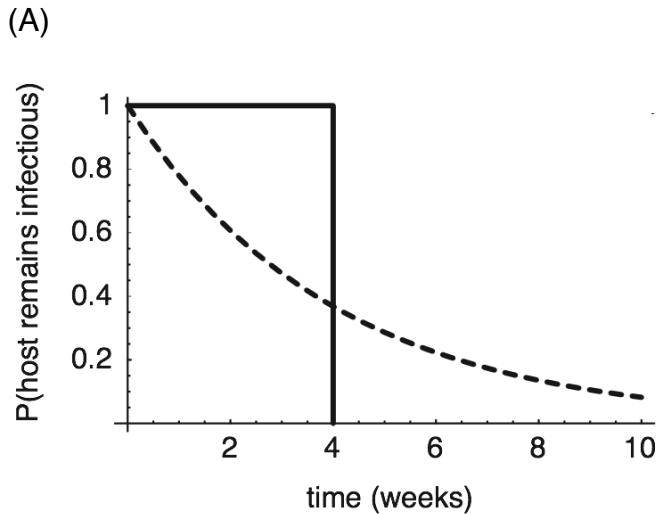


Figure 7

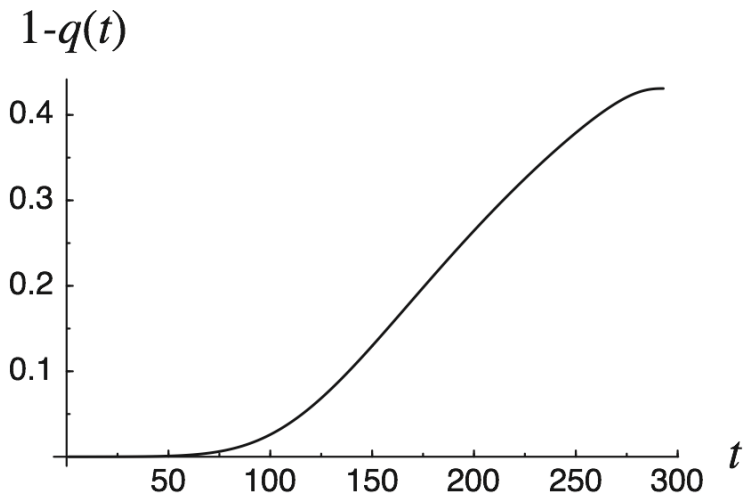
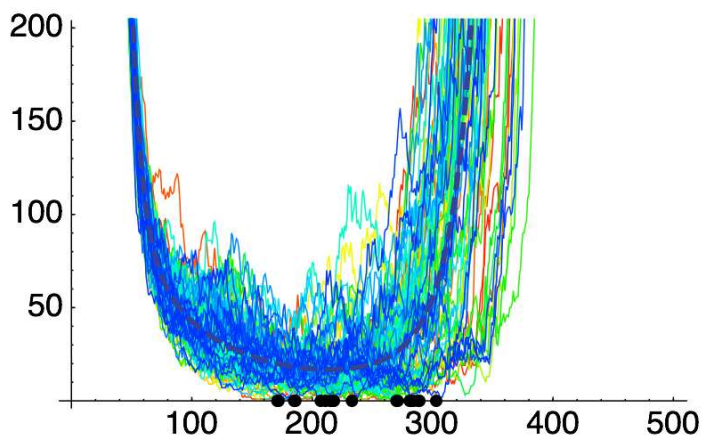


Figure 8

(A)



(B)

